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## Multiply a Fraction by a Whole Number Using Models

Essential Question How can you use a model to multiply a fraction by a whole number?

Fractions-4.NF.B.4b Also 4.NF.B.4c MATHEMATICAL PRACTICES MP1, MP2, MP4

## Unlock the Problem

Rafael practices the violin for $\frac{3}{4}$ hour each day. He has a recital in 3 days. How much time will he practice in 3 days?

Example 1 use a model to multiply $3 \times \frac{3}{4}$.
Think: $3 \times \frac{3}{4}$ is 3 groups of $\frac{3}{4}$ of a whole. Shade the model to show 3 groups of $\frac{3}{4}$.


1 group of $\frac{3}{4}=$ $\qquad$
2 groups of $\frac{3}{4}=$ $\qquad$
3 groups of $\frac{3}{4}=$ $\qquad$
$3 \times \frac{3}{4}=$ $\qquad$
So, Rafael will practice for $\qquad$ hours in all.

- How many equal groups of $\frac{3}{4}$ should you model?


Reason Abstractly If you multiply $4 \times \frac{2}{6}$, is the product greater than or less than 4? Explain.

1. Explain how you can use repeated addition with the model to find the product $3 \times \frac{3}{4}$.
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$\qquad$
2. Rafael's daily practice of $\frac{3}{4}$ hour is in sessions that last for $\frac{1}{4}$ hour each. Describe how the model shows the number of practice sessions Rafael has in 3 days.

## 1 <br> Example 2 use a pattern to multiply.

You know how to use a model and repeated addition to multiply a fraction by a whole number. Look for a pattern in the table to discover another way to multiply a fraction by a whole number.

| Multiplication Problem |  |  |  |  | Whole Number <br> (Number of Groups) | Fraction <br> (Size of Groups) | Product |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\frac{1}{6}$ | $\frac{1}{6}$ | $\frac{1}{6}$ | $\frac{1}{6}$ | $\frac{1}{6}$ | $\frac{1}{6}$ |  |  |  |  |
| $\frac{1}{6}$ | $\frac{1}{6}$ | $\frac{1}{6}$ | $\frac{1}{6}$ | $\frac{1}{6}$ | $\frac{1}{6}$ | $2 \times \frac{1}{6}$ |  | 2 | $\frac{1}{6}$ of a whole |
| $\frac{1}{6}$ | $\frac{1}{6}$ | $\frac{1}{6}$ | $\frac{1}{6}$ | $\frac{1}{6}$ | $\frac{1}{6}$ |  |  | $\frac{2}{6}$ |  |
| $\frac{1}{6}$ | $\frac{1}{6}$ | $\frac{1}{6}$ | $\frac{1}{6}$ | $\frac{1}{6}$ | $\frac{1}{6}$ | $2 \times \frac{2}{6}$ |  | 2 | $\frac{2}{6}$ of a whole |
| $\frac{1}{6}$ | $\frac{1}{6}$ | $\frac{1}{6}$ | $\frac{1}{6}$ | $\frac{1}{6}$ | $\frac{1}{6}$ |  |  |  |  |
| $\frac{1}{6}$ | $\frac{1}{6}$ | $\frac{1}{6}$ | $\frac{1}{6}$ | $\frac{1}{6}$ | $\frac{1}{6}$ | $2 \times \frac{3}{6}$ |  | 2 | $\frac{4}{6}$ |

When you multiply a fraction by a whole number, the numerator in the product is the product of the $\qquad$ and the
$\qquad$ of the fraction. The denominator in the product is the same as the $\qquad$ of the fraction.
3. How do you multiply a fraction by a whole number without using a model or repeated addition?
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$\qquad$
4. Describe two different ways to find the product $4 \times \frac{2}{3}$.
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$\qquad$
$\qquad$

Name $\qquad$

## Share and Show

## MATH

BOARD

1. Find the product of $3 \times \frac{5}{8}$.

$$
1 \text { group of } \frac{5}{8}=\frac{}{8}
$$

2 groups of $\frac{5}{8}=\frac{}{8}$
3 groups of $\frac{5}{8}=\frac{}{8}$
$3 \times \frac{5}{8}=$ $\qquad$

## Multiply.

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$2 \times \frac{4}{5}=$ $\qquad$
3.


| $\frac{1}{3}$ | $\frac{1}{3}$ | $\frac{1}{3}$ |
| :---: | :---: | :---: |


| $\frac{1}{3}$ | $\frac{1}{3}$ | $\frac{1}{3}$ |
| :---: | :---: | :---: |

$$
4 \times \frac{2}{3}=
$$

$\qquad$


3 groups of $\frac{5}{8}$
4. $5 \times \frac{3}{10}=$ $\qquad$
5. $4 \times \frac{5}{6}=$ $\qquad$

MATHEMATICAL PRACTICES (4)

## Model Mathematics

 Describe how to model Exercise 5.
## On Your Own

## Multiply.

6. $2 \times \frac{7}{12}=$ $\qquad$
7. $6 \times \frac{3}{8}=$ $\qquad$
8. $5 \times \frac{2}{4}=$
9. $3 \times \frac{4}{6}=$ $\qquad$ 10. $2 \times \frac{5}{10}=$ $\qquad$ 11. $4 \times \frac{2}{8}=$
$\qquad$
$\qquad$

## (aticicici 7 Look for a Pattern Algebra Write the unknown number.

12. 

$\times \frac{2}{3}=\frac{12}{3}$
13. $5 \times \frac{}{4}=\frac{10}{4}$
14. $2 \times \frac{7}{\square}=\frac{14}{8}$

## Unlock the Problem

15. 

THINK SMARTER
Lisa makes clothes for pets.
She needs $\frac{5}{6}$ yard of fabric to make 1 dog coat. How much fabric does she need to make 3 dog coats?
a. What do you need to find?

b. What information do you need?
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c. Show the steps you use to solve the problem.
d. Complete the sentence.

Lisa needs $\qquad$ yards of fabric to make 3 dog coats.
16. GODEFPER Manuel's small dog eats $\frac{2}{4}$ bag of dog food in 1 month. His large dog eats $\frac{3}{4}$ bag of dog food in 1 month. How many bags do both dogs eat in 6 months?
17. THINKSMARTER Select the correct product for the equation.

$6 \times \frac{4}{7}=\square$
$8 \times \frac{3}{12}=\square$

## Multiply a Fraction by a Whole Number Using Models

Common
Core COMMON CORE STANDARD-4.NF.B. 4
Build fractions from unit fractions by applying and extending previous understandings of operations on whole numbers..

## Multiply.

1. $2 \times \frac{5}{6}=$ $\qquad$
2. $3 \times \frac{2}{5}=$ $\qquad$ 3. $7 \times \frac{3}{10}=$ $\qquad$

3. $3 \times \frac{5}{12}=$ $\qquad$
4. $6 \times \frac{3}{4}=$ $\qquad$
5. $4 \times \frac{2}{5}=$ $\qquad$

## Problem Solving

7. Matthew walks $\frac{5}{8}$ mile to the bus stop each morning. How far will he walk in 5 days?
8. Emily uses $\frac{2}{3}$ cup of milk to make one batch of muffins. How many cups of milk will Emily use if she makes 3 batches of muffins?
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9. WRITE Math Explain how you can use a model to find $4 \times \frac{3}{8}$. Include a drawing and a solution.
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$\qquad$
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## Lesson Check (4.N.B.4b)

1. Aleta's puppy gained $\frac{3}{8}$ pound each week for 4 weeks. Altogether, how much weight did the puppy gain during the 4 weeks?
2. Pedro mixes $\frac{3}{4}$ teaspoon of plant food into each gallon of water. How many teaspoons of plant food should Pedro mix into 5 gallons of water?

## Spiral Review (4.NF.A.2, 4.NF.B.3b, 4.NF.B.3c, 4.NF.B.4a)

3. Ivana has $\frac{3}{4}$ pound of hamburger meat. She makes 3 hamburger patties. Each patty weighs the same amount. How much does each hamburger patty weigh?
4. Lance wants to find the total length of 3 boards. He uses the expression $3 \frac{1}{2}+\left(2+4 \frac{1}{2}\right)$. How can Lance rewrite the expression using both the Associative and Commutative Properties of Addition?
5. Write $\frac{7}{10}$ as a sum of fractions two different ways.
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6. Fill in the blank with a symbol that makes this statement true:

